The right core inverses of a product and a companion matrix

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Abstract: In this paper, characterizations of right core inverse by one-sided invertibility are given. The necessary and sufficient conditions, which guarantee that *paq* have right core inverses are investigated. Furthermore, characterizations of right core inverses of triangular matrices, 2×2 matrices and a companion matrix are considered.

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